

Extremely high electron mobility in isotopically-enriched ²⁸Si two-dimensional electron gases grown by chemical vapor deposition

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Both depletion-mode and enhancement-mode two-dimensional electron gases (2DEGs) in isotopically enriched ²⁸Si with extremely high mobility ($522\,000\,\text{cm}^2/\text{V}$ s) are presented. The samples were grown by chemical vapor deposition using enriched silane. The fraction of the spin-carrying isotope ²⁹Si was reduced to the level of 800 ppm by ²⁸Si enrichment, with the electron spin dephasing time expected to be as long as 2 μ s. Remote impurity charges from ionized dopants and the Si/Al₂O₃ interface were suggested to be the dominant source for electron scattering in the enriched ²⁸Si 2DEGs. © 2013 AIP Publishing LLC. [http://dx.doi.org/10.1063/1.4824729]

Quantum dots (QDs) containing single electrons are very promising for the realization of spin-based quantum computing in solid-state systems due to the maturity of semiconductor technology.¹ The short dephasing time $T_2^* \sim 7$ ns of electron spins² in GaAs QDs due to the strong hyperfine interactions with the host nuclei³ imposes an upper limit on the duration of a gate switching event, in order to preserve the quantum phase information before a gate switching operation is completed. A longer dephasing time (~360 ns) of electron spins was demonstrated⁴ in silicon with a natural abundance of the ²⁹Si isotope (4.7%), which carries nuclear spins.⁵

To go beyond the limit of natural Si, in this Letter, we report depletion- and enhancement-mode Si two-dimensional electron gases (2DEG) with the ²⁹Si depleted to only 1.7% of its natural abundance, for an absolute level of 0.08%. The transport properties were measured at cryogenic temperatures, with a high mobility of 522 000 cm²/V s, among the best reported of any type of modulation-doped Si 2DEGs grown by chemical vapor deposition (CVD). Based on a model of spin decoherence in Si,⁶ we estimated the upper limit of spin dephasing time to be 2 μ s in such structures.

In this work, polished relaxed Si_{0.73}Ge_{0.27} buffers with a graded Si_{1-x}Ge_x layer (0 < x < 0.27) and a Si_{0.73}Ge_{0.27} layer grown on Si (100) substrates were used for the epitaxial growth of silicon 2DEGs. The preparation steps of wafers and the precursors for epitaxial growth were described elsewhere.⁷ After cleaning steps, a SiGe relaxed buffer layer of 100–150 nm was grown at 575 °C, followed by a strained-Si layer (2DEG layer) at 625 °C, a SiGe setback layer at 575 °C, a n-type SiGe supply layer at 575 °C, and a SiGe cap layer at 575 °C, followed by a strained Si cap layer at 625 °C (Table I) for depletion-mode 2DEGs. All layers above the polished relaxed buffers were grown using diluted silane of enriched ²⁸Si with respect to other isotopes. For enhancement-mode 2DEGs, the structure was the same, except that there was no setback or doped layer, the SiGe cap was either 60 or 150 nm,

and the enriched silane was used only for the growth of Si quantum well.

The concentrations of three isotopes, ²⁸Si, ²⁹Si, and ³⁰Si, and Ge, vs. depth in a depletion mode sample are shown in Fig. 1. Below the growth interface at a depth of 185 nm, the fractions of ²⁸Si, ²⁹Si, and ³⁰Si are 92, 4.7, and 3.3%, respectively, which are the natural isotopic abundances of silicon.⁵ For Si and SiGe epitaxial layers grown with silane of enriched ²⁸Si, the fractions for those three isotopes become 99.72, 0.08, and 0.002%, respectively. The ratios of ²⁸Si to ²⁹Si, are 20 and 1250 in the natural and enriched silicon, respectively (a $60 \times$ increase). The ²⁸Si to ³⁰Si ratio increases from 27 to 50 000 (2000 × increase). The electron transport properties of Si 2DEG samples were characterized by low-temperature Hall measurement (at 4 K and 0.3 K). For the depletion-mode device, the sample was first mesa-etched to define a Hall bar geometry, and then Ohmic contacts were made by AuSb (1% Sb) deposition followed by rapid thermal annealing at 450 °C for 10 min. For enhancement-mode devices, Ohmic contacts were first made by ion implantation of phosphorus followed by furnace annealing at 600 °C for 1 h.⁸ Then, an Al₂O₃ gate insulator of 90 nm was deposited at 300 °C by atomic layer deposition (ALD) with a metal gate of Cr/Au on top. Longitudinal resistance (R_{xx}) and Hall resistance (R_{xy}) were measured at 4K for all samples and at 0.3 K for the depletion-mode device using the low-frequency ac lock-in technique.

Before growing device structures with the isotopicallyenriched silane, we grew depletion-mode structures with normal silane to find densities and structures with high mobility. The sample structure and growth conditions were similar to those in Table I, although the SiGe setback thickness and other layers were varied slightly. A summary plot of Hall mobility vs. density at 4 K from ungated Hall bars is shown in Fig. 2, with squares representing the data from unenriched silane. Highest mobilities were observed in the density range of $4-6 \times 10^{11}$ cm⁻². Below this density (achieved with a thicker SiGe setback layer), the decreasing electron mobility results from less electron screening, which is a stronger (negative) effect than the positive effect of moving the ionized dopants farther from the 2DEG. A dotted line fit to the data

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TABLE I. Epitaxial layer structures and growth temperatures of depletionmode and enhancement-mode enriched ²⁸Si 2DEG samples.

Layer (nm)	Growth temperature (°C)	Depletion-mode (modulation-doped)	Enhancement-mode (undoped)
Si cap	625	7	3
SiGe cap	575	25	60 or 150
SiGe supply	575	10	0
(P doping level)		$(4 \times 10^{18} \text{cm}^{-3})$	(no doping)
SiGe setback	575	25	0
Si quantum well	625	16	9 ^a
SiGe re-growth	575	110	150

 $^{\mathrm{a}}\mathrm{For}$ enhancement-mode devices, $^{28}\mathrm{Si}$ was enriched only in the Si quantum well layer.

shows a relationship of $\mu \propto n^{1.5}$. This is consistent with prior work^{9,10} which suggested that with an exponent of 1.5, remote impurity scattering from the modulation-doped supply layer is the dominant scattering mechanism at low densities. On the other hand, as the electron density increases above $6 \times 10^{11} \text{ cm}^{-2}$ (by reducing the setback distance), the mobility drops. This has been attributed to the stronger scattering induced by a shorter setback distance, which compromises the effects of electron screening.¹¹

The depletion-mode samples with enriched ²⁸Si were designed to have a density in the range of maximum mobility as shown in Fig. 2 (4–6 × 10^{11} cm⁻²). The data points of these samples are plotted as stars in Fig. 2, along with the data for the natural Si 2DEGs. The trends of mobility vs. density are remarkably consistent, with the exception of one sample for unknown reasons. The highest Hall mobility observed among enriched-²⁸Si samples at 4 K was 399 000 cm²/V s with a density of 4 × 10^{11} cm⁻².

One sample (that of Table I) was chosen for measurements at 0.3 K. At 4 K, its Hall electron density is 4×10^{11} cm⁻² and the Hall mobility is 399 000 cm²/V s. At 0.3 K, the longitudinal (R_{xx}) and transverse (Hall) resistances (R_{xy}) were also measured with the magnetic field up to 8 T (Fig. 3). The onset of Shubnikov-de Haas (SdH) oscillations in R_{xx} occurs at 0.4 T. The spin splitting due to the associated Zeeman energy difference exceeding the Landau level broadening occurs at 0.75 T with a filling factor of $\nu = 24$.



FIG. 1. Concentrations of silicon isotopes 28 Si, 29 Si, and 30 Si, and Ge vs. depth in a 2DEG structure by SIMS measurements. The growth was started at a depth of 185 nm, and the S QW is at a depth of 75 nm.



FIG. 2. Hall electron mobility vs. density for various ungated depletionmode (modulation-doped) Si 2DEGs grown in our lab. Stars represent the data of isotopically-enriched ²⁸Si 2DEGs and squares are the data from Si 2DEGs of natural isotopic abundance.

The revelation of two-fold degeneracy from two valleys of density of states was observed at 1.9 T with $\nu = 9$. For Hall resistance (R_{xy}), the quantum Hall structures can be resolved at B = 0.7 T at $\nu = 24$ and clear plateaus were observed at $\nu = 2$, 4, 8, etc. The two-dimensional electron densities extracted from SdH oscillations and low-field Hall resistance were 4.02 and 4.18×10^{11} cm⁻², respectively showing that parallel conduction is insignificant. The electron mobility of this device at 0.3 K is 522 000 cm²/V s, corresponding to an associated mean free path of 6 μ m. This mobility may be the highest reported for modulation-doped Si 2DEGs grown by CVD regardless of ²⁸Si enrichment. In previous work of isotopically-enriched ²⁸Si 2DEGs grown by molecular beam epitaxy, the highest reported mobility was 55 000 cm²/V-s.¹²

Enhancement-mode samples with enriched ²⁸Si only in the Si QW layer were made without n-type dopants with a SiGe setback layer of 60 or 150 nm on top of the 2DEG layer (Table I). With a metal gate of Cr/Au on top of 90-nm Al₂O₃, the Hall electron density increased with gate voltage and mobility increased rapidly with electron density (Fig. 4). The effective gate capacitance extracted from the slopes of n_{2D} vs. V_g are 5.8×10^{-8} F/cm² and 4.1×10^{-8} F/cm² for the setback layers of 60 and 150 nm (Fig. 4(a)), respectively, within 5% of the calculated values based on a parallel-plate capacitor model. The lowest densities are 1.1 and



FIG. 3. Magneto-resistances of a depletion-mode enriched ²⁸Si 2DEG device measured at 0.3 K. Electron density $(4 \times 10^{11} \text{ cm}^{-2})$ and mobility (522 000 cm²/V s) were extracted from the periods of Shubnikov-de Haas oscillations in longitudinal resistance (R_{xx}) vs. (1/B) and its value at zero field.

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FIG. 4. (a) Electron density vs. gate voltage by Hall measurement at 4 K for enhancement-mode enriched ²⁸Si 2DEGs with a SiGe cap layer of 60 or 150 nm, and (b) mobility vs. density for these two devices at 4 K, along with dotted lines representing a power law relation between mobility and density. The lowest observed density was $6 \times 10^{10} \, \mathrm{cm}^{-2}$ for a 150 nm SiGe cap layer.

 $0.6 \times 10^{11} \text{ cm}^{-2}$ at $V_g = 2.2 \text{ V}$, which we believe is the lowest density among all reported enriched ²⁸Si 2DEGs. At lower gate voltages, there was no conduction in the 2DEG channel because of the metal-insulator transition (MIT).¹³

In the enhancement-mode devices without ²⁸Si enrichment, a higher mobility is possible by increasing the SiGe setback layer between Si surface and the 2DEG layer.¹⁴ However, we chose our structures of 60 to 150 nm because a thickness of ~100 nm is preferred for the precise lateral gate control over the underlying 2DEG for quantum dot applications. In both samples, the mobility scales with the density as $\mu \propto n^{1.7}$. This is close to the exponent of 1.5 in a theoretical model⁸ when the 2DEG mobility is limited by the remote impurity scattering. In contrast, when the background impurity scattering dominates, the exponent is expected to be unity.⁸ Thus, the mobility in the enhancement mode devices appears to be limited by remote impurity scattering, presumably impurity charges at the Si/Al₂O₃ interface.

We now estimate the potential impact of a ²⁹Si level of 0.08% on electron decoherence in Si QDs. By reducing the ²⁹Si level to < 50 ppm, a lower spin decoherence rate of electrons bound to phosphorus donors in isotopically enriched ²⁸Si has been demonstrated experimentally.¹⁵ In QDs, a similar effect is expected. Assuming a Si QD of 10⁵ nuclei Assali *et al.*⁶ have predicted a dephasing time T_2^* given by



FIG. 5. Dephasing time of electron spins in silicon quantum dots vs. ²⁹Si fraction. The solid line is the model prediction by Assali,⁶ and the solid square represents data in QDs made in naturally occurring-Si.⁴ If the spin decoherence was due solely to nuclear hyperfine interactions, the expected dephasing time for a ²⁹Si fraction of 0.08% (dotted lines, ²⁹Si level of this work) would be 2 μ s. The dephasing time (~7 ns) of GaAs QDs² is also shown for comparison.

$$T_2^* = \frac{10^{11}\hbar}{4.3eV \cdot \sqrt{10^5}r},\tag{1}$$

where *r* is the atomic fraction of ²⁹Si. The predicted dephasing time versus *r* is shown in Fig. 5 and compared with experimental results. Maune *et al.* reported a dephasing time of 360 ns in double QDs in Si of natural abundance,⁴ which is very close to Assali's model prediction. In our samples, the fraction of ²⁹Si is ~ 0.08% (vertical line in Fig. 5) and the dephasing time is expected to be $2 \mu s$. For comparison, a much shorter dephasing time of 7 ns in GaAs QDs² was also labeled, showing a great promise of isotopically-enriched ²⁸Si 2DEGs for achieving low electron spin decoherence rates in Si QDs.

In summary, we report high quality depletion-mode and enhancement-mode 2DEGs in silicon grown by CVD from silane in which the ²⁹Si level was reduced to 0.08%. Such a level may lead to an electron dephasing time in silicon quantum dots as long as 2 μ s. A mobility of 522 000 cm²/V s was observed in a depletion-mode device. In enhancement-mode devices, a low electron density of 6×10^{10} cm⁻² before the metal-insulator transition was demonstrated by gating. In both depletion- and enhancement-mode devices, a strikingly similar dependence of mobility on density was seen, suggesting remote impurities limit the mobility in both cases.

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